

## Formulae For Memorization / Reference

### (A) Conversion Factors

$$1 \text{ m} = 39.370 \text{ inch} = 3.28084 \text{ ft} = 1.09361 \text{ yd} = 0.00062137 \text{ mile}$$

$$1 \text{ inch} = 0.025400 \text{ m} = 2.5400 \text{ cm}$$

$$1 \text{ km/h} = (1/3.600) \text{ m/s}; = 0.62137 \text{ mi/h}; = 0.911342 \text{ ft/s};$$

$$1 \text{ m/s} = 3.600 \text{ km/h}; = 2.23694 \text{ mi/h}; = 3.2808 \text{ ft/s};$$

$$1 \text{ mi/h} = 1.46667 \text{ ft/sec} = 0.44704 \text{ m/s} = 1.60935 \text{ km/h}$$

$$1 \text{ ft/sec} = 0.68182 \text{ mi/h} = 0.30480 \text{ m/s} = 1.097283 \text{ km/h}$$

$$1 \text{ km} = 1 \times 10^3 \text{ m} \quad 1 \text{ cm} = 1 \times 10^{-2} \text{ m} \quad 1 \text{ mm} = 1 \times 10^{-3} \text{ m} \quad 1 \mu\text{m} = 1 \times 10^{-6} \text{ m}$$

$$1 \text{ mile} = 1609.344 \text{ m} = 6.3360 \times 10^4 \text{ in} = 5280 \text{ ft} = 1760 \text{ yds} = 8 \text{ furlong}$$

$$1 \text{ cm} = 1 \times 10^{-2} \text{ m} \quad 1 \text{ cm}^2 = 1 \times 10^{-4} \text{ m}^2 \quad 1 \text{ cm}^3 = 1 \times 10^{-6} \text{ m}^3$$

$$1 \text{ year} = 365 \text{ days} = 8760 \text{ hrs} = 525,600 \text{ min} = 31536000 \text{ sec}$$

$$T_{spin, earth} = 24 \text{ hrs} \quad v_{spin} \sim 1670 \text{ km/h} \sim 1037 \text{ mi/h}$$

$$T_{orbit, earth} = 365 \text{ days} \quad v_{orbit} \sim 30,000 \text{ km/h} \sim 18,560 \text{ mi/h}$$

$$\pi = 3.141593 \quad (\text{and not just } 3.14) \quad 1 \text{ radian} = 57.29578^\circ \quad 1^\circ = 0.0174533 \text{ radian}$$

$$1 \text{ rpm} = 2\pi/60 = 0.1047198 \text{ rad/sec} = 2\pi r/60 \text{ m} = (0.1047198)(r) \text{ m}$$

### B) Perimeters

$$\text{Circle of radius } r \text{ (circumference):} \quad 2\pi r = \pi d \quad (d = 2r)$$

$$\text{Square of side } l: \quad 4l$$

$$\text{Rectangle of length } l \text{ and width } w: \quad 2(l + w)$$

$$\text{Trapezoid of lengths and widths } l_1, l_2, w_1, w_2: \quad l_1 + w_1 + l_2 + w_2$$

$$\text{Triangle of sides } a, b, c: \quad (a + b + c)$$

### C) Diagonals

$$\text{Square of side } l: \quad (\sqrt{2})(l) \quad \text{Rectangle of length } l \text{ and width } w: \quad \sqrt{(l^2 + w^2)}$$

### D) Half Diagonals

$$\text{Square of side } l: \quad l/\sqrt{2} \quad \text{Rectangle of length } l \text{ and width } w: \quad (1/2)\sqrt{(l^2 + w^2)}$$

### E) Areas

$$\text{Circle of radius } r: \quad \pi r^2 = (\pi/4)d^2 = 0.785398d^2 \quad \text{Square of side } l: \quad l^2$$

$$\text{Rectangle of length } l \text{ and width } w: \quad l \times w \quad \text{Parallelogram} \quad (a)(b)(\sin\theta)$$

$$\text{Triangle of base } a \text{ and height } h: \quad (1/2)(a)(h)$$

$$\text{Trapezoid of base } l_1 \text{ and heights } w_1, w_2: \text{ base } \times \text{ average height} = \quad (l_1)\left(\frac{w_1 + w_2}{2}\right)$$

$$\text{Surface of a sphere of radius } r: \quad 4\pi r^2 = \pi d^2$$

$$\text{surface of a cylinder of radius } r \text{ and height } h: \quad (2\pi r)(r + h)$$

### F) Volumes

$$\text{Sphere of radius } r: \quad (4/3)\pi r^3 = 4.1888r^3 = 0.523599d^3 \quad \text{Cubic Box of side } l: \quad l^3$$

$$\text{Rectangular Box of length } l, \text{ width } w \text{ and height } h: \quad l \times w \times h$$

$$\text{Cylinder of radius } r \text{ and height } h: \quad (\pi r^2)(h)$$

**G) Trigonometry**

$$\sin \theta = \text{opposite/hypotnuse} \quad \cos \theta = \text{adjacent/hypotnuse} \quad \tan \theta = \text{opposite/adjacent} = \sin \theta / \cos \theta$$

$$\sin^2 \theta + \cos^2 \theta = 1 \quad \sec^2 \theta - \tan^2 \theta = 1 \quad \csc^2 \theta - \cot^2 \theta = 1$$

$$\sin 2\theta = 2 \sin \theta \cos \theta \quad \cos 2\theta = \cos^2 \theta - \sin^2 \theta = 2 \cos^2 \theta - 1 = 1 - 2 \sin^2 \theta \quad \tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$$

$$\sin(-\theta) = -\sin \theta \quad \cos(-\theta) = \cos \theta \quad \tan(-\theta) = -\tan \theta$$

$$\sin(90 + \theta) = \cos \theta \quad \sin(90 - \theta) = \cos \theta \quad \sin(180 - \theta) = \sin \theta \quad \sin(180 + \theta) = -\sin \theta$$

$$\cos(90 + \theta) = -\sin \theta \quad \cos(90 - \theta) = \sin \theta \quad \cos(180 + \theta) = -\cos \theta \quad \cos(180 - \theta) = -\cos \theta$$

$$\tan(90 + \theta) = -\cot \theta \quad \tan(90 - \theta) = \cot \theta$$

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B \quad \cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B} \quad \sin\left(\frac{\theta}{2}\right) = \sqrt{\frac{1 - \cos \theta}{2}} \quad \cos\left(\frac{\theta}{2}\right) = \sqrt{\frac{1 + \cos \theta}{2}} \quad \tan\left(\frac{\theta}{2}\right) = \sqrt{\frac{1 - \cos \theta}{1 + \cos \theta}}$$

$$\sin A \pm \sin B = 2 \sin\left(\frac{A \pm B}{2}\right) \cos\left(\frac{A \mp B}{2}\right) \quad \cos A + \cos B = 2 \cos\left(\frac{A + B}{2}\right) \cos\left(\frac{A - B}{2}\right)$$

$$\cos A - \cos B = 2 \sin\left(\frac{A + B}{2}\right) \sin\left(\frac{B - A}{2}\right)$$

$$(\cos A)(\cos B) = \left(\frac{1}{2}\right)[\cos(A + B) + \cos(A - B)] \quad (\sin A)(\sin B) = \left(\frac{1}{2}\right)[\cos(A - B) - \cos(A + B)]$$

**H) Pythagorean Theorem**

$$(\text{adjacent})^2 + (\text{opposite})^2 = (\text{hypotenuse})^2 \quad \theta = \tan^{-1} (\text{opposite} / \text{adjacent})$$

**I) Quadratic Equation**

$$ax^2 + bx + c = 0 \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad \sqrt{b^2 - 4ac} = \text{discriminant}$$

$$x^2 + 2\beta x + \gamma = 0 \quad x = -\beta \pm \sqrt{\beta^2 - \gamma}$$

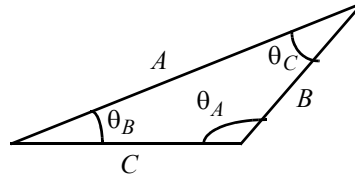
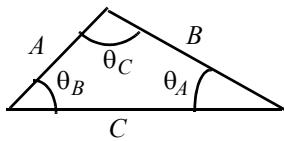
**J) Triangles: Sine and Cosine Laws**

If triangles of sides  $A, B, C$  and  $A', B', C'$  are similar, then  $A/A' = B/B' = C/C'$

For any triangle of sides  $A, B, C$  and angles  $\theta_A, \theta_B, \theta_C$ :

$$\text{cosine law: } A^2 = B^2 + C^2 - 2BC \cos \theta_A \quad \cos \theta_A = (B^2 + C^2 - A^2)/(2BC)$$

$$\text{sine law: } A/(\sin \theta_A) = B/(\sin \theta_B) = C/(\sin \theta_C)$$

**K) Algebra**

$$(a + b)^2 = a^2 + b^2 + 2ab \quad (a - b)^2 = a^2 + b^2 - 2ab \quad (a^2 - b^2) = (a + b)(a - b)$$

$$\log(ab) = \log a + \log b \quad \log(a/b) = \log a - \log b \quad \log a^n = n \log a$$

$$\ln(ab) = \ln a + \ln b \quad \ln(a/b) = \ln a - \ln b \quad \ln a^n = n \ln a$$

**L) All exponents and trigonometric functions are dimensionless numbers!**


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